

Lab 1: Mathematical Foundations

Math 124, Fall 2026 at the University of Michigan

due by the end of your lab section on Wednesday, September 2nd, 2026

Name: _____

username: _____

Welcome to the first lab of Math 124!

Each lab worksheet will contain several activities, most of which will involve writing math on paper, and some of which will involve running code in a Jupyter Notebook. Lab activities are meant to last an hour, and the second hour of lab is dedicated to starting the homework assignment. To receive credit for a lab, you must show your lab TA your work on both the lab worksheet and homework assignment.

While you must get checked off by your lab TA **individually**, we encourage you to form groups with 1-2 other students to complete the activities together.

Activity 1: Hello World!

In this class and in labs, collaboration is key because together groups can accomplish much more than individuals can on their own.

First, introduce yourself to two people in the class and exchange contact information. Write down their names and contact information below.

Person 1

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Person 2

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Next, pair up with one or two other students and solve the following cross-number crossword puzzle, adapted from the [Berkeley Math Tournament 2023](#). Each spot in the grid should be filled with a digit from 0 to 9 using the clues below. Digits may be repeated.

A	B	C
D		
E		

- A Across: A number with only even digits, in strictly descending order (3)
D Across: A number not divisible by 9 (3)
E Across: A number divisible by 11 (2)
A Down: A number with consecutive digits, in ascending order (3)
B Down: A number where the product of the lesser-valued two digits is equal to the largest digit (3)
C Down: A prime number greater than 10 (2)

After you solve the puzzle, compare your thinking with the rest of your group. Write one insight that someone else in your group had that you did not think of.

Overview: Sets and set-builder notation

The material here is a summary of [Chapter 1.2](#) of the course notes.

A **set** is a well-defined collection of distinct objects. For example,

$$A = \{2, 4, 6, 8\}$$

is the set of even numbers between 2 and 8. The numbers 2, 4, 6, and 8 are the **elements** of A . We write $2 \in A$ and $3 \notin A$. Sets do not contain duplicates, so $\{2, 2, 4, 6, 6\}$ is not a valid set. Sets do not keep track of order, so

$$\{2, 4, 6\} = \{6, 4, 2\}.$$

Set-builder notation describes a set by stating a rule that all of its elements follow. Its general form is

$$\{\text{what goes in the set} : \text{condition}\}.$$

For example, if $A = \{2, 4, 6, 8\}$, then the set $C = \{6, 12, 18, 24\}$ can be described as

$$C = \{3x : x \in A\}.$$

More examples:

1. $\{x : x \in C, x > 10\}$ is the set of elements of C that are greater than 10.
2. $\{10, 20, 30, \dots, 100\}$ can be expressed in set-builder notation as

$$\{10x : x \in \mathbb{Z}, 1 \leq x \leq 10\}.$$

$\mathbb{Z}$ is the set of all **integers**.

3. $\{x : x \in \mathbb{Z}, x \geq 0\}$ is the set of all non-negative integers.
4. $\{(x, y) : x^2 + y^2 = 16, x \in \mathbb{R}, y \in \mathbb{R}\}$ is the set of all points on the circle with radius 4 centered at $(0, 0)$. $\mathbb{R}$ refers to the set of **real numbers**.

In many of these examples, the item before the colon $:$ was simply x , and following the colon were multiple conditions on x , one of which was the set we were selecting elements from to create our new set (e.g. C , $\mathbb{Z}$, or $\mathbb{R}$). There is a shorter notation that is often used for sets like these:

- $\{x : x \in C, x > 10\}$ can be shortened to $\{x \in C : x > 10\}$.
- $\{x : x \in \mathbb{Z}, x \geq 0\}$ can be shortened to $\{x \in \mathbb{Z} : x \geq 0\}$.

In general, the two forms you'll see are:

$$\{f(x) : \text{conditions on } x\}$$

$$\{x \in S : \text{conditions on } x\}$$

Activity 2: Sets and subsets

- a) Write the set $\{k \in \mathbb{Z} : |k + 1| < 5\}$ using enumerative notation.

- b) Write the set $\{2, 5, 10, 17, 26, 37, \dots\}$ using set-builder notation. Try doing so in at least two different ways, each using a different formula before the colon.

A set B is a **subset** of a set A if every element of B is also an element of A , written $B \subseteq A$.

- c) Let $A = \{x \in \mathbb{Z} : x > 2\}$ and $B = \{x \in \mathbb{Z} : x > 6\}$. Is $A \subseteq B$? Is $B \subseteq A$? Both? Neither?

- d) Let $C = \{x \in \mathbb{R} : x^2 > 4\}$ and $D = \{x \in \mathbb{R} : x > 2\}$. Explain why it is **not true** that $C \subseteq D$ by finding one element in C that is not in D .

Activity 3: Mathematical Hygiene

One of the main learning objectives in this course is to develop proper mathematical **hygiene** — that is, writing clear solutions using proper mathematical grammar and correctly stating assumptions.

a) The “proof” below shows that $0 = 1$.

1	Suppose $a = b$. Then,
2	$a^2 = ab$
3	$a^2 - b^2 = ab - b^2$
4	$(a - b)(a + b) = b(a - b)$
5	$a + b = b$
6	$2b = b$
7	$2 = 1$
8	$1 = 0$

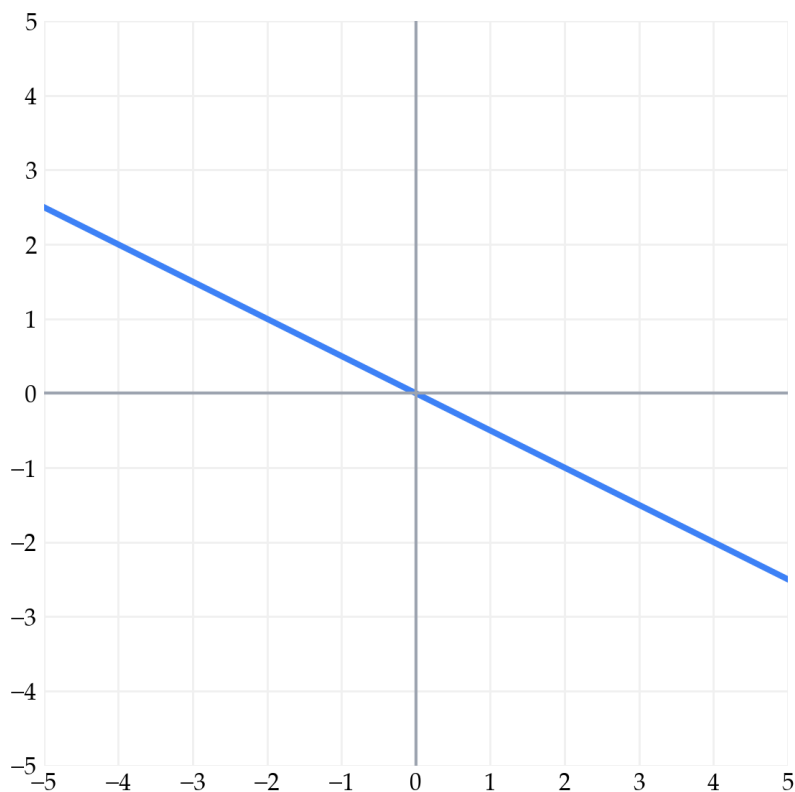
Identify the line on which a mistake is first made and explain what the mistake is.

b) Express the set of solutions x to the inequality below in set-builder notation.

$$\frac{-3x + 2}{7} \leq 5$$

Activity 4: (Set)ting the Stage

Find the equation of the line below. Then, describe the set of all points (x, y) that satisfy the equation in set-builder notation.

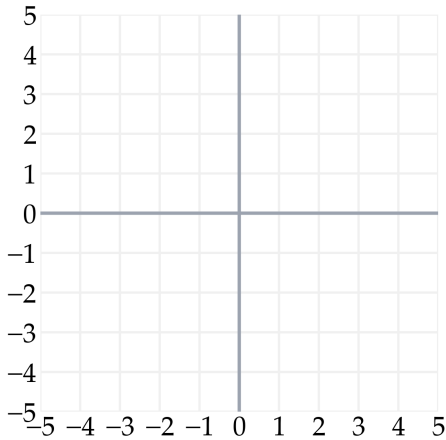


Activity 5: Parallel and Perpendicular Lines

Consider the line

$$5x - 4y = 12.$$

- a) Plot the line on the axes below.



- b) Find an equation for a line that is parallel to this line.

- c) Find an equation for a line that is perpendicular to this line.

- d) Find the point where this line intersects with the line

$$y = x - 2.$$

Activity 6: Programming Activity

Most homeworks and some labs will have a Jupyter Notebook, containing Python code that supplements our understanding of the relevant mathematical ideas of the week.

To open the notebook for Lab 1, click the Google Colab link under "Code" on the course website for Lab 1. Instructions on how to use Google Colab are at math124.org/running-code. If you are viewing the lab worksheet after it has been posted, [this](#) direct link will work, too.

To receive credit for the programming component of the lab, work through the entire notebook and show your lab TA the graph you create at the very bottom, with your name in it.